

Question # 5 of 10 ( Start time: 09:59:29 AM, 18 February 2021 )

Total Marks: 1

A compact set in  $\mathbb{R}^n$  is ----- .

Select the correct option

[Reload Math Equations](#)

open and unbounded



open and bounded



closed and unbounded



closed and bounded



Question # 7 of 10 ( Start time: 10:00:13 AM, 18 February 2021 )

Total Marks: 1

In  $\mathbb{R}^n$ , an open  $n$  - ball of radius  $r$  about  $X_0$  is  $B_r(X_0) = \{X : |X - X_0| < r\}$ , then its closure is - - - - - .

Select the correct option



$$\{X : |X - X_0| = r\}$$



$$\{X : |X - X_0| \leq r\}$$



$$\{X : |X - X_0| \geq r\}$$



$$\{X : |X - X_0| > r\}$$



Question # 10 of 10 ( Start time: 10:01:14 AM, 18 February 2021 )

Total Marks: 1

In  $\mathbb{R}^2$ , the set  $\{(x, y) : (x^2 + y^2 \leq a) \vee (x^2 + y^2 \geq b), a < b\}$  is a region.

Select the correct option

[Reload Math Equations](#)

True



False

If  $\mathbb{R}^n$  is connected, such that  $\mathbb{R}^n = A \cup B$  with  $\bar{A} \cap B = A \cap \bar{B} = \phi$ , then - - - - .

Select the correct option

 Reload Math Equations



$$\bar{A} \subset A, \bar{B} \subset B$$



$A$  and  $B$  are both open and closed



Either  $A = \mathbb{R}^n, B = \phi$  or  $B = \mathbb{R}^n, A = \phi$



All above can be concluded





## MTH631:Quiz-2

Question # 6 of 10 ( Start time: 09:56:07 AM, 18 February 2021 )

If  $\lim_{X \rightarrow X_0} f(X)$  exists, then it is \_\_\_\_\_.

Select the correct option

<input type="radio"/>	1
<input checked="" type="radio"/>	unique
<input type="radio"/>	0
<input type="radio"/>	none of these



Question # 3 of 10 ( Start time: 09:54:16 AM, 18 February 2021 )

Sequence in  $\mathbb{R}^2$  defined as;

$$\{X_r\} = \left\{ \left( \frac{\cos r}{r}, \frac{\sin r}{r} \right) \right\} \text{ converges to } \text{-----}.$$

Select the correct option

- |                                  |        |
|----------------------------------|--------|
| <input checked="" type="radio"/> | (1, 0) |
| <input type="radio"/>            | (0, 1) |
| <input type="radio"/>            | (0, 0) |
| <input type="radio"/>            | (1, 1) |



Question # 8 of 10 ( Start time: 09:56:56 AM, 18 February 2021 )

An open disc:  $\{(x, y) : x^2 + y^2 < 1\}$  in  $\mathbb{R}^2$  is - - - - - .

Select the correct option

<input checked="" type="radio"/>	disconnected
<input type="radio"/>	disconnected polygonally
<input type="radio"/>	connected polygonally
<input type="radio"/>	none of these.



Question # 10 of 10 ( Start time: 09:57:27 AM, 18 February 2021 )

In  $\mathbb{R}^n$ , if the line segment:  $X = tX_2 + (1 - t)X_1$ ,  $0 < t < 1$ , joining  $X_1$  and  $X_2$  lies in  $S_\epsilon(X_0)$ , then — — —.

Select the correct option



$$|X - X_0| < \epsilon$$



$$|X - X_0| < 1 - \epsilon$$



$$|X - X_0| < t$$



$$|X - X_0| < 1 - t$$



Set of isolated point(s) of the complement of set  $\{(x, y) : -n < x, y < n, (x, y) \neq (0, 0), n \in \mathbb{N}\}$  in  $\mathbb{R}^2$ , is — — — —.

Select the correct option

<input type="radio"/>	$\{(x, y) \in \mathbb{R}^2 : x = y =  n , n \in \mathbb{N}\} \cup \{(0, 0)\}$
<input checked="" type="radio"/>	$\{(0, 0)\}$
<input type="radio"/>	$\{(x, y) \in \mathbb{R}^2 : x = y =  n , n \in \mathbb{N}\} \cap \{(0, 0)\}$
<input type="radio"/>	$\{(x, y) \in \mathbb{R}^2 : x = y =  n , n \in \mathbb{N}\}$

In  $\mathbb{R}^3$ , the lines  $L_1 : X = (2, -1, 5) + \alpha (2, -1, 3)$  and  $L_2 : X = (2, -1, 5) + \beta \left( -5, \frac{5}{2}, -\frac{15}{2} \right)$  are traversed in ----- directions, where  $-\infty < \alpha, \beta < \infty$ .

Select the correct option

<input checked="" type="radio"/>	same
<input type="radio"/>	opposite
<input type="radio"/>	perpendicular
<input type="radio"/>	oblique



Question # 5 of 10 ( Start time: 09:55:47 AM, 18 February 2021 )

The function  $f(x, y) = \frac{xy}{x^2 + y^2}$  is defined everywhere in \_\_\_\_\_ except at \_\_\_\_\_.

Select the correct option

<input type="radio"/>	$R^2, (1, -1)$
<input type="radio"/>	$R^3, (1, -1, 0)$
<input checked="" type="radio"/>	$R^2, (0, 0)$
<input type="radio"/>	none of these



## MTH631:Quiz-2

Question # 7 of 10 ( Start time: 09:56:28 AM, 18 February 2021 )

If  $\phi \neq S \subseteq \mathbb{R}^n$ , then the set  $S$  is bounded if-----.

Select the correct option

<input type="radio"/>	$\sup \{ X - Y  : X, Y \in S\} = \infty$
<input checked="" type="radio"/>	$\sup \{ X - Y  : X, Y \in S\} < \infty$
<input type="radio"/>	$\inf \{ X - Y  : X, Y \in S\} = \infty$
<input type="radio"/>	$\inf \{ X - Y  : X, Y \in S\} < \infty$



Question # 9 of 10 ( Start time: 09:57:13 AM, 18 February 2021 )

The space  $R^n$  is \_\_\_\_\_.


Select the correct option

<input checked="" type="radio"/>	connected
<input type="radio"/>	not connected
<input type="radio"/>	both a and b
<input type="radio"/>	none of these



For a non empty closed and bounded subset  $S$  in  $\mathbb{R}^n$ , if  $H$  is the collection open sets such that  $S \subset \cup \{H : H \in H\}$ , then by Heine - Borel theorem,

Select the correct option

<input type="radio"/>	$S \subset \bigcup_{\lambda \in \Lambda} \{H_\lambda : H_\lambda \in H\}$
<input type="radio"/>	$S \subset \bigcup_{\alpha=1}^{\infty} \{H_\alpha : H_\alpha \in H\}$
<input type="radio"/>	$S \subset \bigcup_{\alpha=1}^n \{H_\alpha : H_\alpha \in H\}$
	All above are equally valid



Question # 7 of 10 ( Start time: 09:44:01 AM, 18 February 2021 )

Total Marks: 1

Limit points of set  $S = \{(x, y) : -n < x, y < n, (x, y) \neq (0, 0), n \in \mathbb{N}\}$  in  $\mathbb{R}^2$ , — — —.

▶ Select the correct option

[Reload Math Equations](#)

$$\{(0, 0)\} \cup \{(x, y) : x, y = \pm n, n \in \mathbb{N}\}$$



$$\{(0, 0)\} \cup S$$



$$\{(0, 0)\} \cup \{(x, y) : x, y = \pm n, n \in \mathbb{N}\} \cup S$$



$$\{(x, y) : x, y = \pm n, n \in \mathbb{N}\} \cup S$$

Question # 6 of 10 ( Start time: 09:43:25 AM, 18 February 2021 )

Total Marks: 1

If  $\lim_{X \rightarrow X_0} f(X)$  exists, then it is \_\_\_\_.

Select the correct option

[Reload Math Equations](#)

<input type="radio"/>	1
<input checked="" type="radio"/>	unique
<input type="radio"/>	0
<input type="radio"/>	none of these

[Click to Save Answer & Move to Next Question](#)



Closure of the set  $\{(x, y) : -n < x, y < n, (x, y) \neq (0, 0), n \in \mathbb{N}\}$  in  $\mathbb{R}^2$ , is — — — —.

Select the correct option

 Reload Math Equations



$$\{(x, y) : -n < x, y < n, n \in \mathbb{N}\}$$



$$\{(x, y) : -n \leq x, y \leq n, n \in \mathbb{N}\}$$



$$\{(x, y) : (x, y) \neq (0, 0)\}$$



$$\{(x, y) : x, y \leq n, (x, y) \neq (0, 0), n \in \mathbb{N}\}$$

Exterior of the set  $\{(x, y) : -n < x, y < n, (x, y) \neq (0, 0), n \in \mathbb{N}\}$  in  $\mathbb{R}^2$ , is — — — —.

Select the correct option

 Reload Math Equations



$$\{(x, y) \in \mathbb{R}^2 \mid |x| < n, |y| > n, n \in \mathbb{N}\}$$



$$\{(x, y) \in \mathbb{R}^2 \mid |x| > n, |y| < n, n \in \mathbb{N}\}$$



$$\{(x, y) \in \mathbb{R}^2 \mid |x| > n, |y| > n, n \in \mathbb{N}\}$$



$$\{(x, y) \in \mathbb{R}^2 \mid |x| < n, |y| < n, n \in \mathbb{N}\}$$

Click to Save Answer & Move to Next Question



In  $\mathbb{R}^n$ , an open  $n$ -ball of radius  $r$  about  $X_0$  is  $B_r(X_0) = \{X : |X - X_0| < r\}$ , which contains -----.

an  $\varepsilon$ -neighborhood of each of its points



limit points of each of its points

only its isolated point at center  $X_0$


limit points of each of its boundary

Question # 2 of 10 ( Start time: 09:04:48 AM, 18 February 2021 )

Total Marks: 1

Limit points of set  $S = \{(x, y) : -n < x, y < n, (x, y) \neq (0, 0), n \in \mathbb{N}\}$  in  $\mathbb{R}^2$ , — — —.

Select the correct option

 Reload Math Equations☒

$$\{(0, 0)\} \cup \{(x, y) : x, y = \pm n, n \in \mathbb{N}\}$$

☐

$$\{(0, 0)\} \cup S$$

☐

$$\{(0, 0)\} \cup \{(x, y) : x, y = \pm n, n \in \mathbb{N}\} \cup S$$

☐

$$\{(x, y) : x, y = \pm n, n \in \mathbb{N}\} \cup S$$



Which of the following non - empty subset on Real line  $\mathbb{R}$  is taken as *region* ?

Select the correct option

 Reload Math Equations



Natural numbers  $\mathbb{N}$



Intervals (open, closed, semi open or closed)



Rationals  $\mathbb{Q}$  or Irrationals  $\mathbb{Q}^c$



Range of pointwise or uniform real valued convergent sequences

MTH631:Quiz-2

Question # 10 of 10 ( Start time: 09:43:48 PM, 17 February 2021 )

The function  $f(x, y) = \frac{xy}{x^2 + y^2}$  is defined everywhere in \_\_\_\_\_ except at \_\_\_\_\_.

Select the correct option

<input type="radio"/>	$R^2, (1, -1)$
<input type="radio"/>	$R^3, (1, -1, 0)$
<input checked="" type="radio"/>	$R^2, (0, 0)$
<input type="radio"/>	none of these

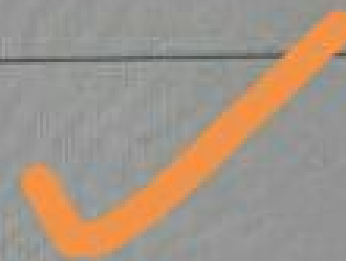


9 of 10 ( Start time: 09:43:10 PM, 17 February 2021 )

In  $\mathbb{R}^n$ , if the line segment:  $X = tX_2 + (1 - t) X_1$ ,  $0 < t < 1$ , joining  $X_1$  and  $X_2$  lies in  $S_\epsilon (X_0)$ , then

correct option

$$|X - X_0| < \epsilon$$



$$|X - X_0| < 1 - \epsilon$$

$$|X - X_0| < t$$

$$|X - X_0| < 1 - t$$

Intervals  $(0,1)$  and  $(1,2)$  are example of disconnected sets in  $\mathbb{R}$  because - - - - - .

$$(0,1) \cap (1,2) = \phi$$

$$\{\text{closure of } (0,1)\} \cap (1,2) = \phi \text{ and } \{\text{closure of } (1,2)\} \cap (0,1) = \phi$$






Question # 7 of 10 ( Start time: 09:41:51 PM, 17 February 2021 )

Let  $f(x, y) = \frac{xy}{x^2 + y^2}$  then the limit of  $f$  along the line  $y = -x$  as  $(x, y)$  approach  $(0, 0)$  is \_\_\_\_\_.

Select the correct option


<input type="radio"/>	0
<input type="radio"/>	undefined
<input type="radio"/>	1/2
<input type="radio"/>	-1/2



Question # 6 of 10 ( Start time: 09:41:19 PM, 17 February 2021 )

For a non empty closed and bounded subset  $S$  in  $\mathbb{R}^n$ , if  $H$  is the collection open sets such  
 $S \subset \bigcup \{H : H \in H\}$ , then by Heine - Borel theorem,

Select the correct option


- |                       |   |
|-----------------------|---|
| <input type="radio"/> | $S \subset \bigcup_{\lambda \in \Lambda} \{H_\lambda : H_\lambda \in H\}$ |
| <input type="radio"/> | $S \subset \bigcup_{\alpha=1}^{\infty} \{H_\alpha : H_\alpha \in H\}$     |
| <input type="radio"/> | $S \subset \bigcup_{\alpha=1}^n \{H_\alpha : H_\alpha \in H\}$            |
| <input type="radio"/> | All above are equally valid   |
- 



Question # 5 of 10 ( Start time: 09:40:39 PM, 17 February 2021 )

An open disc:  $\{(x, y) : x^2 + y^2 < 1\}$  in  $\mathbb{R}^2$  is - - - - - .

Select the correct option

- |                       |                          |
|-----------------------|--------------------------|
| <input type="radio"/> | diconnected              |
| <input type="radio"/> | disconnected polygonally |
| <input type="radio"/> | connected polygonally    |
| <input type="radio"/> | none of these.           |
- 

# 4 of 10 ( Start time: 09:40:07 PM, 17 February 2021 )

Exterior of the set  $\{(x, y) : -n < x, y < n, (x, y) \neq (0, 0), n \in \mathbb{N}\}$  in  $\mathbb{R}^2$ , is — — — —.

The correct option

Re

$$\{(x, y) \in \mathbb{R}^2 \mid |x| < n, |y| > n, n \in \mathbb{N}\}$$

$$\{(x, y) \in \mathbb{R}^2 \mid |x| > n, |y| < n, n \in \mathbb{N}\}$$

$$\{(x, y) \in \mathbb{R}^2 \mid |x| > n, |y| > n, n \in \mathbb{N}\}$$

$$\{(x, y) \in \mathbb{R}^2 \mid |x| < n, |y| < n, n \in \mathbb{N}\}$$





Question # 3 of 10 ( Start time: 09:39:20 PM, 17 February 2021 )

A sequence of points  $\{X_r\}$  in  $R^n$  converges if and only if for each \_\_\_\_\_ there is an integer  $K$  such that \_\_\_\_\_ if  $r, s \geq K$ .

Select the correct option

<input type="radio"/>	$\varepsilon < 0,  X_r - X_s  < \varepsilon$
<input type="radio"/>	$\varepsilon > 0,  X_r - X_s  > \varepsilon$
<input checked="" type="radio"/>	$\varepsilon > 0,  X_r - X_s  < \varepsilon$
<input type="radio"/>	$\varepsilon \neq 0,  X_r - X_s  > \varepsilon$

Question # 2 of 10 ( Start time: 09:38:28 PM, 17 February 2021 )

If  $\lim_{X \rightarrow X_0} f(X)$  exists, then it is \_\_\_\_.

Select the correct option

<input type="radio"/>	1
<input checked="" type="radio"/>	unique
<input type="radio"/>	0
<input type="radio"/>	none of these




MTH631:Quiz-2

Question # 1 of 10 ( Start time: 09:37:10 PM, 17 February 2021 )


A compact set in  $\mathbb{R}^n$  is -----.

Select the correct option

<input type="radio"/>	open and unbounded
<input type="radio"/>	open and bounded
<input type="radio"/>	closed and unbounded
<input type="radio"/>	closed and bounded

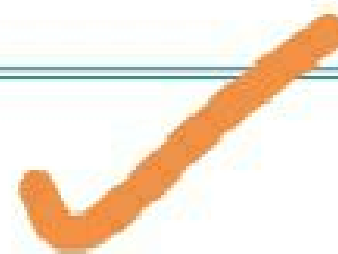


Closure of the set  $\{(x, y) : -n < x, y < n, (x, y) \neq (0, 0), n \in \mathbb{N}\}$  in  $\mathbb{R}^2$ , is — — — —.

 Reload Math Equa

$$\{(x, y) : -n < x, y < n, n \in \mathbb{N}\}$$

$$\{(x, y) : -n \leq x, y \leq n, n \in \mathbb{N}\}$$




$$\{(x, y) : (x, y) \neq (0, 0)\}$$

$$\{(x, y) : x, y \leq n, (x, y) \neq (0, 0), n \in \mathbb{N}\}$$



Interior of the set  $\{(x, y) : -n < x, y < n, (x, y) \neq (0, 0), n \in \mathbb{N}\}$  in  $\mathbb{R}^2$ , is — — — —.

ion

 Reload Math Eq

$$\{(x, y) \in \mathbb{R}^2 \mid |x| < n, |y| > n, n \in \mathbb{N}\}$$

$$\{(x, y) \in \mathbb{R}^2 \mid |x| > n, |y| < n, n \in \mathbb{N}\}$$

$$\{(x, y) \in \mathbb{R}^2 \mid |x| > n, |y| > n, n \in \mathbb{N}\}$$

$$\{(x, y) \in \mathbb{R}^2 \mid |x| < n, |y| < n, n \in \mathbb{N}\}$$



Question # 9 of 10 ( Start time: 09:31:00 PM, 17 February 2021 )

If  $H$  is an open covering of a compact subset  $S$ , then  $S$  can be covered by \_\_\_\_\_ many sets from  $H$ .

Select the correct option

 Reload

<input checked="" type="radio"/>	finitely
<input type="radio"/>	infinitely
<input type="radio"/>	both a and b
<input type="radio"/>	non of these



Set of isolated point(s) of the complement of set  $\{(x, y) : -n < x, y < n, (x, y) \neq (0, 0), n \in \mathbb{N}\}$  in  $\mathbb{R}^2$ , is -

Correct option

$$\{(x, y) \in \mathbb{R}^2 : x = y = |n|, n \in \mathbb{N}\} \cup \{(0, 0)\}$$

$$\{(0, 0)\}$$


$$\{(x, y) \in \mathbb{R}^2 : x = y = |n|, n \in \mathbb{N}\} \cap \{(0, 0)\}$$


$$\{(x, y) \in \mathbb{R}^2 : x = y = |n|, n \in \mathbb{N}\}$$

Question # 9 of 10 ( Start time: 09:29:43 PM, 17 February 20

The space  $R^n$  is \_\_\_\_\_.

Select the correct option

<input type="radio"/>	connected
<input type="radio"/>	not connected
<input type="radio"/>	both a and b
<input type="radio"/>	none of these





A set " S " is polygonally connected if, ----- pair of points in S can be connected by a polygonal path lying ----- in " S ".

Select the correct option



some, entirely



every , entirely



some, partially



every, partially



Question # 8 of 10 ( Start time: 09:29:10 PM, 17 February 2021 )

If  $\phi \neq S \subseteq \mathbb{R}^n$ , then the set  $S$  is bounded if - - - - - .

Select the correct option

<input type="radio"/>	$\sup \{ X - Y  : X, Y \in S\} = \infty$
<input checked="" type="radio"/>	$\sup \{ X - Y  : X, Y \in S\} < \infty$
<input type="radio"/>	$\inf \{ X - Y  : X, Y \in S\} = \infty$
<input type="radio"/>	$\inf \{ X - Y  : X, Y \in S\} < \infty$



The function  $f(x, y) = \frac{xy}{x^2 + y^2}$  is defined everywhere in \_\_\_\_\_ except at \_\_\_\_\_.

Select the correct option

 Reload Math



$R^2, (1, -1)$



$R^3, (1, -1, 0)$



$R^2, (0, 0)$

none of these



In  $\mathbb{R}^n$ , which of the following is true about  $\phi = \{\}$  and  $A = \{(a_1, a_2, \dots, a_n), a_i \in \mathbb{R}, 1 \leq i \leq n, i \in \mathbb{N}\}$ ?

Select option

[Reload Math Equation](#)

$\phi$  is Disconnected and  $A$  is Connected

$\phi$  is Connected and  $A$  is Disconnected

Both are Connected

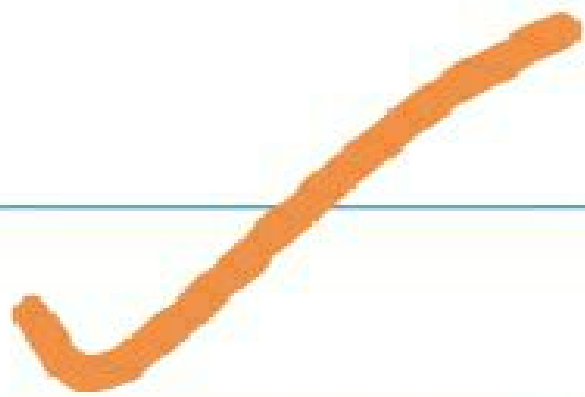
Both are Disconnected



An open disc:  $\{(x, y) : x^2 + y^2 < 1\}$  in  $\mathbb{R}^2$  is - - - - - .

Select the correct option

Relo



diconnected



disconnected polygonally



connected polygonally



none of these.



Boundary of the set  $\{(x, y) : -n < x, y < n, (x, y) \neq (0, 0), n \in \mathbb{N}\}$  in  $\mathbb{R}^2$ , is — — —

Select the correct option

 Reload Math

☒  $\{(x, y) \in \mathbb{R}^2 \mid x = \pm n, y = \pm n, n \in \mathbb{N}\} \cup \{(0, 0)\}$


☐  $\{(x, y) \in \mathbb{R}^2 \mid x = \pm n, y = \pm n, n \in \mathbb{N}\}$

☐  $\{(0, 0)\}$

☐  $\{(x, y) \in \mathbb{R}^2 \mid x = \pm n, y = \pm n, n \in \mathbb{N}\} \cap \{(0, 0)\}$

In  $\mathbb{R}^n$ , if the line segment:  $X = tX_2 + (1 - t)X_1$ ,  $0 < t < 1$ , joining  $X_1$  and  $X_2$  lies in  $S_\varepsilon(X_0)$ , then — — —.

One correct option

 Reload Math Equation

$$|X - X_0| < \varepsilon$$



$$|X - X_0| < 1 - \varepsilon$$

$$|X - X_0| < t$$

$$|X - X_0| < 1 - t$$

If  $H$  is an open covering of a compact subset  $S$ , then  $S$  can be covered by \_\_\_\_\_ many sets from  $H$ .

Select the correct option


 Reload Math Equations

<input checked="" type="radio"/>	finitely
<input type="radio"/>	infinitely
<input type="radio"/>	both a and b
<input type="radio"/>	non of these



Set of isolated point(s) of the complement of set  $\{(x, y) : -n < x, y < n, (x, y) \neq (0, 0), n \in \mathbb{N}\}$  in  $\mathbb{R}^2$ , is — — — —.

Select the correct option

 Reload Math Equations


<input type="radio"/>	$\{(x, y) \in \mathbb{R}^2 : x = y =  n , n \in \mathbb{N}\} \cup \{(0, 0)\}$
<input checked="" type="radio"/>	$\{(0, 0)\}$
<input type="radio"/>	$\{(x, y) \in \mathbb{R}^2 : x = y =  n , n \in \mathbb{N}\} \cap \{(0, 0)\}$
<input type="radio"/>	$\{(x, y) \in \mathbb{R}^2 : x = y =  n , n \in \mathbb{N}\}$

Question # 2 of 10 ( Start time: 09:25:12 PM, 17 February 2021 )

Total Marks: 1

A sequence of points  $\{X_r\}$  in  $R^n$  converges if and only if for each \_\_\_\_\_ there is an integer  $K$  such that \_\_\_\_\_ if  $r, s \geq K$ .

Select the correct option

 Reload Math Equations



$$\varepsilon < 0, |X_r - X_s| < \varepsilon$$



$$\varepsilon > 0, |X_r - X_s| > \varepsilon$$



$$\varepsilon > 0, |X_r - X_s| < \varepsilon$$



$$\varepsilon \neq 0, |X_r - X_s| > \varepsilon$$

Start time: 09:24:35 PM, 17 February 2021 )

In  $\mathbb{R}^n$ , which of the following is true about  $\phi = \{\}$  and  $A = \{(a_1, a_2, \dots, a_n), a_i \in \mathbb{R}, 1 \leq i \leq n, i \in \mathbb{N}\}$ ?

ption

 Reload M

$\phi$  is Disconnected and  $A$  is Connected

$\phi$  is Connected and  $A$  is Disconnected

Both are Connected

Both are Disconnected





Limit points of set  $S = \{(x, y) : -n < x, y < n, (x, y) \neq (0, 0), n \in \mathbb{N}\}$  in  $\mathbb{R}^2$ , — — —.

ion

 Reload Mat

$$\{(0, 0)\} \cup \{(x, y) : x, y = \pm n, n \in \mathbb{N}\}$$

$$\{(0, 0)\} \cup S$$

$$\{(0, 0)\} \cup \{(x, y) : x, y = \pm n, n \in \mathbb{N}\} \cup S$$



$$\{(x, y) : x, y = \pm n, n \in \mathbb{N}\} \cup S$$

Click to Save Answer & Move to Next Question

In  $\mathbb{R}^n$ , a function  $f$  is differentiable at  $X_0$ ,  $\Leftrightarrow \exists$  a linear function  $L$  in a way that  $f(X) - f(X_0)$  can be approximated near  $X_0$  by  $L$  satisfying;

Select the correct option

 Reload Math Equations



$$L(X - X_0) = LX - LX_0$$



$$L(XX_0) = (LX)(LX_0)$$



$$L\left(\frac{X}{X_0}\right) = \frac{LX}{LX_0}, |X_0| \neq 0, LX_0 \neq 0$$



None of the above

Click to Save Answer & Move to Next Question

Question # 9 of 10 ( Start time: 06:15:03 PM, 26 February 2021 )

Total Marks: 1

In  $\mathbb{R}^n$ , monotonicity, limits inferior and superior of sequences, and divergence to  $\pm \infty$  are undefined for  $n > 1$  because  $\mathbb{R}^n$  is - - - - - .

Select the correct option

Reload Math Equations

<input type="radio"/>	complete
<input type="radio"/>	a Field
<input checked="" type="radio"/>	not ordered for $n > 1$
<input type="radio"/>	not compact for $n > 1$



Suppose in  $\mathbb{R}^2$ ,  $f$ ,  $f_x$ ,  $f_y$  and  $f_{xy}$  exist on neighborhood  $N$  of  $(x_0, y_0)$ . Then  $f_{yx}(x_0, y_0)$  exists, and  $f_{yx}(x_0, y_0) = f_{xy}(x_0, y_0)$  because if  $f_{xy}$  is - - - - .

Select the correct option

[Reload Math Equations](#)

bounded



continuous



differentiable



partially differentiable

[Click to Save Answer & Move to Next Question](#)

Question # 2 of 10 ( Start time: 06:11:26 PM, 26 February 2021 )

Total Marks: 1

If  $f$  is continuous on a compact set  $S$  in  $\mathbb{R}^n$ , then  $f$  — — — — on  $S$ .

Select the correct option

[Reload Math Equations](#)

attains all its bounds



is also uniformly continuous



is also defined on all the limit points of "S"



All above are equally valid

[Click to Save Answer & Move to Next Question](#)

A sufficient condition for a function of several variables to be differentiable at point is

Select the correct option

 Reload Math Equations

<input type="radio"/>	only the partial derivative should exists at that point.
<input checked="" type="radio"/>	All partial derivatives exists and are continuous at that point
<input type="radio"/>	only limit at that point should exists.
<input type="radio"/>	None of these



Click to Save Answer & Move to Next Question



Question # 3 of 10 ( Start time: 06:02:18 PM, 26 February 2021 )

Total Marks: 1

$$\lim_{(x,y) \rightarrow (a,b)} \frac{\sin \sqrt{1-x^2-2y^2}}{\sqrt{1-x^2-2y^2}} = 1, \text{ if } \dots\dots\dots$$

Select the correct option

[Reload Math Equations](#)

$$(a^2 + 2b^2) > 1$$



$$(a^2 + 2b^2) < 1$$



$$(a^2 + 2b^2) = 1$$



$$(a^2 + 2b^2) \geq 1$$

[Click to Save Answer & Move to Next Question](#)

Question # 4 of 10 ( Start time: 06:03:04 PM, 26 February 2021 )

Total Marks: 1

$$\text{In } \mathbb{R}^2, f(X) = |X|^2 \text{ and } \Phi = \left( \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}} \right), \text{ then } \frac{\partial f(X)}{\partial \Phi} =$$

Select the correct option

☐

$$\frac{x_1 + x_2}{\sqrt{2}}$$

☐

$$x_1 + x_2$$

☐

$$\frac{x_1 + x_2}{2}$$

☐

$$\sqrt{2}(x_1 + x_2)$$

Question # 8 of 10 ( Start time: 06:05:07 PM, 26 February 2021 )

Total Marks: 1

Let  $f$  be defined and continuous on a region  $S$  in  $\mathbb{R}^n$ . Suppose that  $X_1$  and  $X_2$  are in  $S$  and  $f(X_1) < Y < f(X_2)$ .

Then  $f(X) = Y$  -----  $X$  in  $S$ .

Select the correct option

[Reload Math Equations](#)

for some



for all


[Click to Save Answer & Move to Next Question](#)

In  $\mathbb{R}^2$ ,  $\lim_{(x,y) \rightarrow (2,2)} \frac{\sin(x-y)}{\sqrt{x-y}} = \text{-----}$ .

Select the correct option

 Reload Math Equations

<input type="radio"/>	$\infty$
<input type="radio"/>	1
<input type="radio"/>	$\sqrt{2}$
<input checked="" type="radio"/>	0





Question # 10 of 10 ( Start time: 05:52:21 PM, 26 February 2021 )

Total Marks: 1

How many *third* order partial derivatives of  $g(x, y) = xy + x^2y^3$  exist in  $\mathbb{R}^3$ ?

Select the correct option

[Reload Math Equations](#)

3



6



8



9

[Click to Save Answer & Move to Next Question](#)

The domain of the real valued function  $f : \mathbb{R}^2 \rightarrow \mathbb{R}$  defined and given by;  
 $f(X) = \frac{\sin \sqrt{1 - x^2 - 2y^2}}{\sqrt{1 - x^2 - 2y^2}}$  is ----- of the region by the ellipse  $x^2 + 2y^2 = 1$ .

Select the correct option

 Reload Math Equations

<input type="radio"/>	interior
<input checked="" type="radio"/>	interior and boundary
<input type="radio"/>	exterior
<input type="radio"/>	exterior and boundary



Question # 5 of 10 ( Start time: 05:50:04 PM, 26 February 2021 )

Total Marks: 1

If a function  $f$  is *continuous* on a *compact set*  $S$  in  $\mathbb{R}^n$ , and  $\alpha = \inf_{X \in S} f(X)$ ,  $\beta = \sup_{X \in S} f(X)$ ,  
then  $f(X_1) = \alpha$  and  $f(X_2) = \beta$  — — — — —  $X_1$  and  $X_2$  in  $S$ .

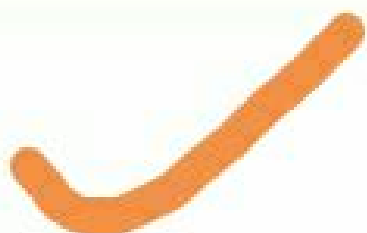
Select the correct option

[Reload Math Equations](#)

for all



for some

[Click to Save Answer & Move to Next Question](#)





In  $\mathbb{R}^n$ ,  $f(X) = \frac{1}{|X - X_0|}$ , and  $\lim_{X \rightarrow X_0} f(X) = \infty$ , then  $f(X) > M > 0 \Rightarrow 0 < |X - X_0| < \delta = \dots$ .

Select the correct option

 Reload Math Equations

<input type="radio"/>	$\frac{1}{\sqrt{M}}$
<input type="radio"/>	$\sqrt{M}$
<input checked="" type="radio"/>	$\frac{1}{M}$
<input type="radio"/>	$M$



Click to Save Answer & Move to Next Question

Question # 4 of 10 ( Start time: 05:49:36 PM, 26 February 2021 )

Total Marks: 1

In  $\mathbb{R}^n$ ,  $\lim_{X \rightarrow X_0} f(X) = -\infty$ , if

Select the correct option

[Reload Math Equations](#)☐

$$\lim_{X \rightarrow X_0} f(-X) = \infty$$

☐

$$\lim_{X \rightarrow X_0} (-f)(X) = \infty$$

☐

$$\lim_{X \rightarrow -X_0} f(X) = \infty$$

☐

$$\lim_{-X \rightarrow X_0} f(X) = \infty$$



Question # 3 of 10 ( Start time: 05:49:04 PM, 26 February 2021 )

Total Marks: 1

In  $\mathbb{R}^n$ , monotonicity, limits inferior and superior of sequences, and divergence to  $\pm \infty$  are undefined for  $n > 1$  because  $\mathbb{R}^n$  is -----.

Select the correct option

[Reload Math Equations](#)

complete



a Field

not ordered for  $n > 1$ not compact for  $n > 1$

Question # 10 of 10 ( Start time: 05:13:08 PM, 26 February 2021 )

Total Marks: 1

In  $\mathbb{R}^n$ , a function  $f$  is differentiable at  $X_0$ ,  $\Leftrightarrow \exists$  a linear function  $L$  in a way that  $f(X) - f(X_0)$  can be approximated near  $X_0$  by  $L$  satisfying  $L(X \pm X_0) = LX \pm LX_0$  such that  $f(X) - f(X_0) = L(X - X_0) + E(X)(|X - X_0|)$  and  $\lim_{X \rightarrow X_0} E(X) = \dots$ .

Select the correct option

[Reload Math Equations](#) $=1$  $>0$  $<0$  $=0$ [Click Here/Answer & Marked Next Question](#)



$$\text{If } g(x, y) = \sqrt{1 - x^2 - 2y^2}, \quad f(t) = \begin{cases} \frac{\sin t}{t}, & t \neq 0 \\ 1, & t = 0 \end{cases},$$

Select the correct option

[Reload Math Equations](#)☐ $\mathbb{R}$ ☐ $\mathbb{R}^3$ ☐ $\{(x, y) : x^2 - 2y^2 \geq 1\}$ ☒ $\{(x, y) : x^2 - 2y^2 \leq 1\}$ [Click to See Answer & Move to Next Question](#)

Question # 3 of 10 ( Start time: 05:08:54 PM, 26 February 2021 )

Total Marks: 1

A set  $A \subset \mathbb{R}$  of real numbers is -----if there exists a real number  $m \in \mathbb{R}$ , such that  $x \geq m$  for every  $x \in A$ .

Select the correct option



bounded below



uniformly continuous



bounded above



None of these



Analogous to the derivative of a function of one variable in  $\mathbb{R}^2$ , the directional derivative of a function  $f$  at  $X_0$  in  $\mathbb{R}^n$  has ----- value(s).

Select the correct option

Relo

<input type="radio"/>	multiple
<input type="radio"/>	infinite many
<input type="radio"/>	unique
<input type="radio"/>	integral

If a function  $f$  is *continuous* on a *compact* set  $S$  in  $\mathbb{R}^n$ , and  $\alpha = \inf_{X \in S} f(X)$ ,  $\beta = \sup_{X \in S} f(X)$ ,  
then  $f(X_1) = \alpha$  and  $f(X_2) = \beta$  — — — — —  $X_1$  and  $X_2$  in  $S$ .

Select the correct option

Relo

for all

for some



Click to Save Answer / Move to Next



$$\text{In } \mathbb{R}^2, f(x, y) = \begin{cases} \frac{\sin \sqrt{1-x^2-2y^2}}{\sqrt{1-x^2-2y^2}}, & x^2 + 2y^2 < 1 \\ 1, & x^2 + 2y^2 = 1 \end{cases}$$

Select the correct option

[Reload Math Equations](#)

continuous



discontinuous

[Click to Save Answer & Move to Next Question](#)

$$\text{In } \mathbb{R}^2, f(X) = |X|^2 \text{ and } \Phi = \left( \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}} \right), \text{ then } \frac{\partial f(X)}{\partial \Phi} =$$

Select the correct option

[Reload Math Equations](#)☒

$$\frac{x_1 + x_2}{\sqrt{2}}$$

☐

$$x_1 + x_2$$

☐

$$\frac{x_1 + x_2}{2}$$

☐

$$\sqrt{2}(x_1 + x_2)$$

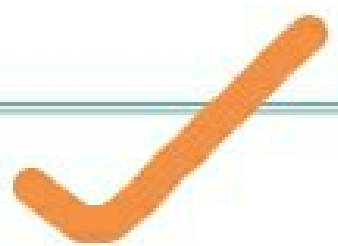
[Click to Save Answer & Move to Next Question](#)

If a function  $f$  is continuous on a Compact set  $S$  in  $\mathbb{R}^n$ , then  $f$  is ----- on  $S$ .

Select the correct option


 Reload Math Equations

<input type="radio"/>	bounded above
<input type="radio"/>	bounded below
<input type="radio"/>	unbounded
<input checked="" type="radio"/>	bounded



$$\text{If } g(x, y) = \sqrt{1 - x^2 - 2y^2}, \quad f(t) = \begin{cases} \frac{\sin t}{t}, & t \neq 0 \\ 1, & t = 0 \end{cases}$$

Select the correct option

 Reload Math Equations



$$\mathbb{R}$$



$$\mathbb{R}^2$$



$$\{(x, y) : x^2 - 2y^2 \geq 1\}$$



$$\{(x, y) : x^2 - 2y^2 \leq 1\}$$



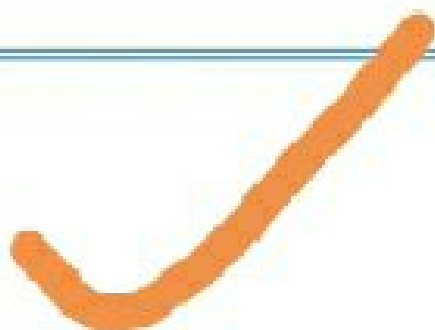
In  $\mathbb{R}^n$ , if the first order partial derivative of a function  $f(X)$  exists at  $X_0$ , then it is essentially continuous at  $X_0$ .

Select the correct option

[Reload Math Equ](#)

☐ True


☒ False

[Click to Save Answer & Move to Next Question](#)



In  $\mathbb{R}^n$ , the function  $f(X)$  is continuous at  $X_0$ , if  $\lim_{X \rightarrow X_0} f(X) = f(X_0)$ , then - - - - - .

Select the correct option

 Reload Math Equations



$X_0$  is in the domain  $D_f$  and limit point of  $D_f$



$X_0$  is in the domain  $D_f$  but not a limit point of  $D_f$



$X_0$  is not in the domain  $D_f$  but a limit point of  $D_f$




neither  $X_0$  is in the domain  $D_f$  nor the limit point of  $D_f$

Click to Save Answer & Move to Next Question

Analogous to the derivative of a function of one variable in  $\mathbb{R}^2$ , the directional derivative of a function  $f$  at  $X_0$  in  $\mathbb{R}^n$  has ----- value(s).

Select the correct option

 Reload Math Equations

<input type="radio"/>	multiple
<input checked="" type="radio"/>	infinite many
<input type="radio"/>	unique
<input type="radio"/>	integral

In  $\mathbb{R}^n$ , monotonicity, limits inferior and superior of sequences, and divergence to  $\pm \infty$  are undefined for  $n > 1$  because  $\mathbb{R}^n$  is - - - - - .

option



Reload M

complete

a Field

not ordered for  $n > 1$



not compact for  $n > 1$

A sufficient condition for a function of several variables to be differentiable at point is

Select the correct option

 Reload Math Equations



only the partial derivative should exists at that point.



All partial derivatives exists and are continuous at that point



only limit at that point should exists.



None of these




Click to Save Answer & Move to Next Question

Let  $f$  be defined on an interval  $I$  in  $\mathbb{R}^2$ . Suppose that  $x_1$  and  $x_2$  are in  $I$  and  $f(x_1) < y < f(x_2)$ .

Then  $f(x) = y$  for some  $x$  in  $I$ .

Select the correct option

 Reload Math Equations

False



True




Click to Save Answer & Move to Next Question



If  $f(x, y, z) = \cos\left(\frac{1}{x^2+2y^2+z^2}\right)$  then  $\lim_{|X| \rightarrow \infty} f(X) = \underline{\hspace{2cm}}$ .

Select the correct option

 Reload Math Equations



1



0



-1



infinite

Click to Save Answer & Move to Next Question

The domain of the real valued function  $f : \mathbb{R}^n \rightarrow \mathbb{R}$  defined and given by;

$$f(X) = (1 - x_1^2 - x_2^2 - \dots - x_n^2)^{-1} \text{ is } \dots\dots\dots$$

Select the correct option

 Reload Math Equations



$$\{X \mid |X| = 1\}$$



$$\{X \mid |X| \neq 1\}$$



Click to Save Answer & Move to Next Question

Question # 8 of 10 ( Start time: 04:56:51 PM, 26 February 2021 )

Total Marks: 1

Identify the false statement(s)

Select the correct option

[Reload Math Equations](#)

The partial derivative is a special case of directional derivative.

For a functions of  $n$  variables

$$f(\mathbf{X})$$

the partial derivative with respect to variable



The partial derivative of the function

$$f(x, y, z) = 3xyz + 2x^2 + z^2$$

with respect to third variable is



None of these

$$\text{In } \mathbb{R}^2, f(x, y) = \begin{cases} \frac{\sin \sqrt{1-x^2-2y^2}}{\sqrt{1-x^2-2y^2}}, & x^2 + 2y^2 < 1 \\ 1, & x^2 + 2y^2 = 1 \end{cases}$$

Select the correct option

[Reload Math Equations](#)

continuous



discontinuous

$$\text{If } g(x, y) = \sqrt{1 - x^2 - 2y^2}, \quad f(t) = \begin{cases} \frac{\sin t}{t}, & t \neq 0 \\ 1, & t = 0 \end{cases}$$

Select the correct option

[Reload Math Equations](#)☐

$\mathbb{R}$

☐

$\mathbb{R}^2$

☐

$\{(x, y) : x^2 - 2y^2 \geq 1\}$

☒

$\{(x, y) : x^2 - 2y^2 \leq 1\}$





If  $f$  is continuous on a compact set  $S$  in  $\mathbb{R}^n$ , then  $f$  — — — — on  $S$ .

Select the correct option

 Reload Math Equations

<input type="radio"/>	attains all its bounds
<input checked="" type="radio"/>	is also uniformly continuous
<input type="radio"/>	is also defined on all the limit points of "S"
<input type="radio"/>	All above are equally valid

Question # 9 of 10 ( Start time: 04:57:28 PM, 26 February 2021 )

Total Marks: 1

If a function  $f$  is continuous on a compact set  $S$  in  $\mathbb{R}^n$ , and  $\alpha = \inf_{X \in S} f(X)$ ,  $\beta = \sup_{X \in S} f(X)$ ,  
then  $f(X_1) = \alpha$  and  $f(X_2) = \beta$  — — — — —  $X_1$  and  $X_2$  in  $S$ .

Select the correct option

[Reload Math Equations](#)

for all



for some



Question # 4 of 10 ( Start time: 04:53:55 PM, 26 February 2021 )

Total Marks: 1

$$\text{In } \mathbb{R}^2, \lim_{(x,y) \rightarrow (2,2)} \frac{\sin(x-y)}{\sqrt{x-y}} = \dots\dots\dots$$

Select the correct option

[Reload Math Equations](#)☐ $\infty$ ☐

1

☐ $\sqrt{2}$ ☒

0

[Click to Go Back Answer & View to Next Question](#)

Question # 10 of 10 ( Start time: 04:58:52 PM, 26 February 2021 )

If a function  $f$  is continuous on a Compact set  $S$  in  $\mathbb{R}^n$ , then  $f$  is ----- on  $S$ .

Select the correct option

Reload Ma

☐

bounded above

☐

bounded below

☐

unbounded

☐

bounded



1.jpg

Jail-Police-Jobs-2...png

In  $\mathbb{R}^n$ , a function  $f$  is differentiable at  $X_0$ ,  $\Leftrightarrow \exists$  a linear function  $L$  in a way that  $f(X) - f(X_0)$  can be approximated near  $X_0$  by  $L$  satisfying;

Select the correct option



$$L(X - X_0) = LX - LX_0$$



$$L(XX_0) = (LX)(LX_0)$$



$$L\left(\frac{X}{X_0}\right) = \frac{LX}{LX_0}, \quad |X_0| \neq 0, LX_0 \neq 0$$



None of the above



1, 26 February 2021 )

$$\lim_{(x,y) \rightarrow (a,b)} \frac{\sin \sqrt{1-x^2-2y^2}}{\sqrt{1-x^2-2y^2}} = 1, \text{ if } \dots\dots\dots$$

$$(a^2 + 2b^2) > 1$$

$$(a^2 + 2b^2) < 1$$

$$(a^2 + 2b^2) = 1$$



$$(a^2 + 2b^2) \geq 1$$

Question # 5 of 10 ( Start time: 05:56:58 PM, 26 February 2021 )

For the function

$$f(x, y) = 3x^2y^3 + xy$$

in two variables,

Select the correct option

<input type="radio"/>	0
<input type="radio"/>	-1
<input type="radio"/>	1
<input type="radio"/>	None of these

Select the correct option

$$f_{yx}(0,0) = \dots\dots\dots$$



0



-1



1



None of these